

# Measurement Error Regression on BMI Data

```
***** bmi2.sas *****
options linesize=79 pagesize = 500 noovp formdlim='_' nodate;
title 'BMI and Health: Use the Double Measurement Design';

data health;
  infile 'bmihealth.data';
  input age1 bml1 fat1 cholest1 diastol1
        age2 bml2 fat2 cholest2 diastol2;
  /* fat1 and fat2 are percent body fat */
  age = (age1+age2)/2; bmi = (bml1+bml2)/2; fat = (fat1+fat2)/2;
  cholest = (cholest1+cholest2)/2 ; diastol = (diastol1+diastol2)/2;

proc calis cov vardef=n;
  /* Analyze the covariance matrix (Default is corr). Divide by n to
   get true MLE of covariance matrix. */
  title2 'Full Model';
  var age1 -- diastol2; /* Name the observed variables */
  /* Now give simultaneous equations, separated by commas. Latent
   variables begin with F for factor. Error terms begin with
   E for error or D for disturbance. SAS is not case sensitive.
   You must name all the parameters. Optional starting values in
   parentheses may be given after the parameters. */
  lineqs
    Fcholest = gammal1 Fage + gammal2 Fbmi + gammal3 Ffat + e1,
    Fdiastol = gamma21 Fage + gamma22 Fbmi + gamma23 Ffat + e2,
    age1      = Fage + delta11,
    bml1      = Fbmi + delta12,
    fat1      = Ffat + delta13,
    age2      = Fage + delta21,
    bml2      = Fbmi + delta22,
    fat2      = Ffat + delta23,
    cholest1  = Fcholest + eps11,
    diastol1  = Fdiastol + eps12,
    cholest2  = Fcholest + eps21,
    diastol2  = Fdiastol + eps22;
  std          /* Variances (not standard deviations) */
    Fage = phill, Fbmi = phi22, Ffat = phi33,
    e1 = psill, e2 = psi22,
    delta11 = TD1_11, delta12 = TD1_22, delta13 = TD1_33,
    delta21 = TD2_11, delta22 = TD2_22, delta23 = TD2_33,
    eps11 = TE1_11, eps12 = TE1_22,
    eps21 = TE2_11, eps22 = TE2_22;
  cov          /* Covariances */
    Fage Fbmi = phi12, Fage Ffat = phi13, Fbmi Ffat = phi23,
    e1 e2 = psi12,
    delta11 delta12 = TD1_12, delta11 delta13 = TD1_13,
    delta12 delta13 = TD1_23,
    delta21 delta22 = TD2_12, delta21 delta23 = TD2_13,
    delta22 delta23 = TD2_23,
    eps11 eps12 = TE1_12,
    eps21 eps22 = TE2_12,
    delta11 eps11 = TDE1_11, delta11 eps12 = TDE1_12,
    delta12 eps11 = TDE1_21, delta12 eps12 = TDE1_22,
    delta13 eps11 = TDE1_31, delta13 eps12 = TDE1_32,
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delta21 eps21 = TDE2_11, delta21 eps22 = TDE2_12,
delta22 eps21 = TDE2_21, delta22 eps22 = TDE2_22,
delta23 eps21 = TDE2_31, delta23 eps22 = TDE2_32;
bounds                                     /* Variances are positive */
    0.0 < phill,   0.0 < phi22,   0.0 < phi33,
    0.0 < psill,   0.0 < psi22,
    0.0 < TD1_11,  0.0 < TD1_22,  0.0 < TD1_33,
    0.0 < TD2_11,  0.0 < TD2_22,  0.0 < TD2_33,
    0.0 < TE1_11,  0.0 < TE1_22,
    0.0 < TE2_11,  0.0 < TE2_22;

/* Now fit a reduced model to test H0: gamma12 = gamma22 = 0,
meaning BMI is unrelated to either cholesterol or blood pressure
if we allow for age and percent body fat. Cut out some long comments.*/

proc calis cov vardef=n;
/* Analyze the covariance matrix (Default is corr). Divide by n to
   get true MLE of covariance matrix. */
title2 'Reduced Model for testing BMI on both DVs';
var agel -- diastol2; /* Name the observed variables */
/* Now give simultaneous equations, separated by commas. Latent
   variables begin with F for factor. Error terms begin with
   E for error or D for disturbance. SAS is not case sensitive.
   You must name all the parameters. Optional starting values in
   parentheses may be given after the parameters. */
lineqs
  Fcholest = gamma11 Fage + gamma12 Fbmi + gamma13 Ffat + e1,
  Fdiastol = gamma21 Fage + gamma22 Fbmi + gamma23 Ffat + e2,
  agel     = Fage + delta11,
  bmi1     = Fbmi + delta12,
  fat1     = Ffat + delta13,
  age2     = Fage + delta21,
  bmi2     = Fbmi + delta22,
  fat2     = Ffat + delta23,
  cholest1 = Fcholest + eps11,
  diastol1 = Fdiastol + eps12,
  cholest2 = Fcholest + eps21,
  diastol2 = Fdiastol + eps22;
std      /* Variances (not standard deviations) */
Fage = phill, Fbmi = phi22, Ffat = phi33,
e1 = psill, e2 = psi22,
delta11 = TD1_11, delta12 = TD1_22, delta13 = TD1_33,
delta21 = TD2_11, delta22 = TD2_22, delta23 = TD2_33,
eps11  = TE1_11, eps12  = TE1_22,
eps21  = TE2_11, eps22  = TE2_22;
cov      /* Covariances */
Fage Fbmi = phi12, Fage Ffat = phi13, Fbmi Ffat = phi23,
e1 e2 = psi12,
delta11 delta12 = TD1_12, delta11 delta13 = TD1_13,
delta12 delta13 = TD1_23,
delta21 delta22 = TD2_12, delta21 delta23 = TD2_13,
delta22 delta23 = TD2_23,
eps11 eps12 = TE1_12,
eps21 eps22 = TE2_12,

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delta11 eps11 = TDE1_11, delta11 eps12 = TDE1_12,
delta12 eps11 = TDE1_21, delta12 eps12 = TDE1_22,
delta13 eps11 = TDE1_31, delta13 eps12 = TDE1_32,
delta21 eps21 = TDE2_11, delta21 eps22 = TDE2_12,
delta22 eps21 = TDE2_21, delta22 eps22 = TDE2_22,
delta23 eps21 = TDE2_31, delta23 eps22 = TDE2_32;
bounds                                     /* Variances are positive */
    0.0 < phi11,   0.0 < phi22,   0.0 < phi33,
    0.0 < psi11,   0.0 < psi22,
    0.0 < TD1_11,   0.0 < TD1_22,   0.0 < TD1_33,
    0.0 < TD2_11,   0.0 < TD2_22,   0.0 < TD2_33,
    0.0 < TE1_11,   0.0 < TE1_22,
    0.0 < TE2_11,   0.0 < TE2_22;
lincon gamma12=0, gamma22=0;
/* Much safer than fitting a model with the variables just missing
in the regression equations. However, SAS will warn us that
"There are 2 active constraints at the solution," and carry on
in a pretty menacing way. The warning can be ignored, in this
particular case where the linear constraints are setting
parameters exactly equal to zero. Do NOT ignore the warning
if an inequality is involved. */
proc iml;
title2 'Calculate Likelihood ratio test of H0: gamma12=gamma22=0';
G = 500 * (0.0391401498-0.0378779129);
pval = 1 - probchi(G,2);
print G,pval;

```

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BMI and Health: Use the Double Measurement Design  
Full Model

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The CALIS Procedure  
Covariance Structure Analysis: Pattern and Initial Values

#### LINEQS Model Statement

	Matrix	Rows	Columns	-----Matrix Type-----
Term 1	1    _SEL_	10	27	SELECTION
	2    _BETA_	27	27	EQSBETA
	3    _GAMMA_	27	15	EQSGAMMA
	4    _PHI_	15	15	SYMMETRIC

#### The 12 Endogenous Variables

Manifest	age1	bmi1	fat1	cholest1	diastoll1	age2
	bmi2	fat2	cholest2	diastol2		
Latent	Fcholest	Fdiastol				

The 15 Exogenous Variables

Manifest					
Latent	Fage	Fbmi	Ffat		
Error	e1	e2	eps11	eps12	eps21
	eps22	delta11	delta12	delta13	delta21
	delta22	delta23			

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BMI and Health: Use the Double Measurement Design  
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The CALIS Procedure  
Covariance Structure Analysis: Pattern and Initial Values

Manifest Variable Equations with Initial Estimates

```
age1      =  1.0000 Fage      +  1.0000 delta11
bmi1     =  1.0000 Fbmi      +  1.0000 delta12
fat1     =  1.0000 Ffat      +  1.0000 delta13
cholest1 =  1.0000 Fcholest +  1.0000 eps11
diastol1 =  1.0000 Fdiastol +  1.0000 eps12
age2     =  1.0000 Fage      +  1.0000 delta21
bmi2     =  1.0000 Fbmi      +  1.0000 delta22
fat2     =  1.0000 Ffat      +  1.0000 delta23
cholest2 =  1.0000 Fcholest +  1.0000 eps21
diastol2 =  1.0000 Fdiastol +  1.0000 eps22
```

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The CALIS Procedure  
Covariance Structure Analysis: Pattern and Initial Values

Latent Variable Equations with Initial Estimates

```
Fcholest =      .*Fage      +      .*Fbmi      +      .*Ffat
                  gamma11          gamma12          gamma13
                  +  1.0000 e1

Fdiastol =      .*Fage      +      .*Fbmi      +      .*Ffat
                  gamma21          gamma22          gamma23
                  +  1.0000 e2
```

**Variances of Exogenous Variables**

Variable	Parameter	Estimate
Fage	phi11	.
Fbmi	phi22	.
Ffat	phi33	.
e1	psi11	.
e2	psi22	.
eps11	TE1_11	.
eps12	TE1_22	.
eps21	TE2_11	.
eps22	TE2_22	.
delta11	TD1_11	.
delta12	TD1_22	.
delta13	TD1_33	.
delta21	TD2_11	.
delta22	TD2_22	.
delta23	TD2_33	.

**Covariances Among Exogenous Variables**

Var1	Var2	Parameter	Estimate
Fage	Fbmi	phi12	.
Fage	Ffat	phi13	.
Fbmi	Ffat	phi23	.
e1	e2	psi12	.
eps11	eps12	TE1_12	.
eps21	eps22	TE2_12	.
eps11	delta11	TDE1_11	.
eps12	delta11	TDE1_12	.
eps11	delta12	TDE1_21	.
eps12	delta12	TDE1_22	.
delta11	delta12	TD1_12	.
eps11	delta13	TDE1_31	.
eps12	delta13	TDE1_32	.
delta11	delta13	TD1_13	.
delta12	delta13	TD1_23	.
eps21	delta21	TDE2_11	.
eps22	delta21	TDE2_12	.
eps21	delta22	TDE2_21	.
eps22	delta22	TDE2_22	.
delta21	delta22	TD2_12	.
eps21	delta23	TDE2_31	.
eps22	delta23	TDE2_32	.
delta21	delta23	TD2_13	.
delta22	delta23	TD2_23	.

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BMI and Health: Use the Double Measurement Design  
Full Model

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The CALIS Procedure  
Covariance Structure Analysis: Maximum Likelihood Estimation

Observations	500	Model Terms	1
Variables	10	Model Matrices	4
Informations	55	Parameters	45

Variable	Mean	Std Dev
age1	43.08800	12.99955
bmi1	25.43580	4.54927
fat1	18.79000	7.75224
cholest1	262.02740	52.50262
diastol1	88.42400	19.27206
age2	44.40600	12.41762
bmi2	25.51760	3.72546
fat2	18.90280	7.56396
cholest2	261.24560	53.87560
diastol2	88.70000	13.08610

NOTE: Some initial estimates computed by two-stage LS method.

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BMI and Health: Use the Double Measurement Design  
Full Model

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The CALIS Procedure  
Covariance Structure Analysis: Maximum Likelihood Estimation

Vector of Initial Estimates

	Parameter	Estimate	Type
1	gamma11	-0.04470	Matrix Entry: _GAMMA_[11:1]
2	gamma12	-6.33575	Matrix Entry: _GAMMA_[11:2]
3	gamma13	4.81865	Matrix Entry: _GAMMA_[11:3]
4	gamma21	0.04906	Matrix Entry: _GAMMA_[12:1]
5	gamma22	-0.29770	Matrix Entry: _GAMMA_[12:2]
6	gamma23	1.43699	Matrix Entry: _GAMMA_[12:3]
7	phi11	147.24427	Matrix Entry: _PHI_[1:1]
8	phi12	8.79461	Matrix Entry: _PHI_[2:1]
9	phi22	12.33537	Matrix Entry: _PHI_[2:2]
10	phi13	27.68039	Matrix Entry: _PHI_[3:1]
11	phi23	22.57943	Matrix Entry: _PHI_[3:2]
12	phi33	45.86815	Matrix Entry: _PHI_[3:3]
13	psi11	2389	Matrix Entry: _PHI_[4:4]
14	psi12	71.22487	Matrix Entry: _PHI_[5:4]
15	psi22	75.27225	Matrix Entry: _PHI_[5:5]
16	TE1_11	192.26932	Matrix Entry: _PHI_[6:6]

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17   TE1_12      39.74295  Matrix Entry: _PHI_[7:6]
18   TE1_22      215.64902  Matrix Entry: _PHI_[7:7]
19   TE2_11      338.32405  Matrix Entry: _PHI_[8:8]
20   TE2_12     -38.53896  Matrix Entry: _PHI_[9:8]
21   TE2_22      15.48280  Matrix Entry: _PHI_[9:9]
22   TDE1_11     -0.37855  Matrix Entry: _PHI_[10:6]
23   TDE1_12      10.18200  Matrix Entry: _PHI_[10:7]
24   TD1_11      21.74398  Matrix Entry: _PHI_[10:10]
25   TDE1_21     -3.46658  Matrix Entry: _PHI_[11:6]
26   TDE1_22      6.35643  Matrix Entry: _PHI_[11:7]
27   TD1_12      1.33004  Matrix Entry: _PHI_[11:10]
28   TD1_22      8.36053  Matrix Entry: _PHI_[11:11]
29   TDE1_31      0.15593  Matrix Entry: _PHI_[12:6]
30   TDE1_32      3.93632  Matrix Entry: _PHI_[12:7]
31   TD1_13     -1.58351  Matrix Entry: _PHI_[12:10]
32   TD1_23      5.78119  Matrix Entry: _PHI_[12:11]
33   TD1_33     14.22915  Matrix Entry: _PHI_[12:12]
34   TDE2_11      1.94395  Matrix Entry: _PHI_[13:8]
35   TDE2_12     -6.39489  Matrix Entry: _PHI_[13:9]
36   TD2_11      6.95289  Matrix Entry: _PHI_[13:13]
37   TDE2_21      2.83802  Matrix Entry: _PHI_[14:8]
38   TDE2_22     -0.80271  Matrix Entry: _PHI_[14:9]
39   TD2_12      0.02965  Matrix Entry: _PHI_[14:13]
40   TD2_22      1.54368  Matrix Entry: _PHI_[14:14]
41   TDE2_31     -2.68759  Matrix Entry: _PHI_[15:8]
42   TDE2_32     -1.99128  Matrix Entry: _PHI_[15:9]
43   TD2_13      2.03567  Matrix Entry: _PHI_[15:13]
44   TD2_23     -1.64710  Matrix Entry: _PHI_[15:14]
45   TD2_33      11.34540  Matrix Entry: _PHI_[15:15]

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BMI and Health: Use the Double Measurement Design  
Full Model

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The CALIS Procedure  
Covariance Structure Analysis: Maximum Likelihood Estimation  
Dual Quasi-Newton Optimization

Dual Broyden - Fletcher - Goldfarb - Shanno Update (DBFGS)

Parameter Estimates	45
Functions (Observations)	55
Lower Bounds	15
Upper Bounds	0

Optimization Start

Active Constraints	0	Objective Function	0.3271903962
Max Abs Gradient Element	0.0798909029		

Iter	Rest arts	Func Calls	Act Con	Objective Function	Obj Change	Fun Gradient	Abs Element	Step Size	Slope Search Direc
1	0	3	0	0.30488	0.0223	0.2450	0.0467	-1.031	
2	0	4	0	0.28493	0.0200	0.1155	0.321	-0.174	
3	0	5	0	0.26868	0.0163	0.0924	1.000	-0.0414	
4	0	7	0	0.21790	0.0508	0.2954	2.854	-0.0371	
5	0	8	0	0.19763	0.0203	0.1178	1.000	-0.0295	
6	0	10	0	0.18967	0.00796	0.0603	1.110	-0.0139	
7	0	12	0	0.18633	0.00334	0.0332	1.482	-0.0039	
8	0	13	0	0.18070	0.00563	0.0151	1.517	-0.0055	
9	0	14	0	0.17263	0.00807	0.0619	1.804	-0.0078	
10	0	15	0	0.16947	0.00316	0.1056	4.513	-0.0045	
11	0	17	0	0.16253	0.00694	0.0414	1.894	-0.0083	
12	0	18	0	0.15246	0.0101	0.0683	3.981	-0.0044	
13	0	20	0	0.14649	0.00597	0.0202	1.567	-0.0072	
14	0	21	0	0.14215	0.00433	0.1391	5.726	-0.0026	
15	0	23	0	0.12979	0.0124	0.0571	3.143	-0.0079	
16	0	24	0	0.12038	0.00941	0.0181	3.313	-0.0093	
17	0	26	0	0.11799	0.00239	0.00639	1.187	-0.0043	
18	0	27	0	0.11522	0.00277	0.0316	7.956	-0.0008	
19	0	29	0	0.10842	0.00680	0.0207	3.239	-0.0043	
20	0	31	0	0.10677	0.00165	0.00901	1.866	-0.0017	
21	0	32	0	0.10409	0.00269	0.0117	3.764	-0.0011	
22	0	33	0	0.10265	0.00143	0.0249	3.013	-0.0022	
23	0	34	0	0.10065	0.00201	0.00890	1.394	-0.0026	
24	0	35	0	0.09993	0.000716	0.0147	5.008	-0.0010	
25	0	36	0	0.09890	0.00103	0.00332	0.942	-0.0019	
26	0	38	0	0.09831	0.000588	0.00738	4.447	-0.0003	
27	0	40	0	0.09319	0.00512	0.00248	12.702	-0.0008	
28	0	42	0	0.09298	0.000213	0.00225	1.906	-0.0002	
29	0	44	0	0.09178	0.00120	0.00948	13.803	-0.0002	
30	0	46	0	0.09106	0.000712	0.00457	1.611	-0.0009	
31	0	47	0	0.09020	0.000866	0.0143	6.590	-0.0003	
32	0	49	0	0.08621	0.00399	0.0242	7.518	-0.0011	
33	0	51	0	0.08430	0.00191	0.00500	1.728	-0.0022	
34	0	53	0	0.08346	0.000838	0.00798	5.288	-0.0003	
35	0	55	0	0.08128	0.00218	0.00609	4.202	-0.0010	
36	0	57	0	0.08104	0.000241	0.00472	1.854	-0.0003	
37	0	59	0	0.07767	0.00338	0.00922	30.705	-0.0002	
38	0	61	0	0.07639	0.00127	0.00196	1.390	-0.0019	
39	0	62	0	0.07594	0.000455	0.00499	8.567	-0.0004	
40	0	63	0	0.07521	0.000729	0.00342	0.835	-0.0014	
41	0	65	0	0.07485	0.000356	0.00379	2.284	-0.0003	
42	0	67	0	0.07157	0.00329	0.00428	18.249	-0.0004	
43	0	69	0	0.07101	0.000553	0.00228	1.309	-0.0008	
44	0	71	0	0.07080	0.000212	0.00318	3.657	-0.0001	
45	0	73	0	0.06998	0.000819	0.00277	7.534	-0.0002	
46	0	75	0	0.06606	0.00392	0.00986	9.447	-0.0008	
47	0	77	0	0.06532	0.000736	0.00178	1.408	-0.0011	
48	0	78	0	0.06525	0.000071	0.00753	10.000	-561E-7	
49	0	80	0	0.06480	0.000451	0.00153	2.125	-0.0004	
50	0	82	0	0.06214	0.00266	0.00382	11.922	-0.0004	
51	0	84	0	0.06208	0.000057	0.00186	1.548	-0.0001	
52	0	86	0	0.06168	0.000402	0.00353	23.010	-351E-7	
53	0	87	0	0.06108	0.000600	0.00145	1.794	-0.0006	

54	0	88	0	0.06054	0.000545	0.00347	4.024	-0.0004
55	0	90	0	0.06021	0.000326	0.000905	1.538	-0.0004
56	0	92	0	0.06017	0.000043	0.00122	1.903	-446E-7
57	0	95	0	0.05838	0.00179	0.0188	118.9	-299E-7
58	0	97	0	0.05783	0.000550	0.00233	1.015	-0.0011
59	0	99	0	0.05775	0.000078	0.00690	3.725	-419E-7
60	0	101	0	0.05745	0.000301	0.00141	6.628	-0.0001
61	0	103	0	0.05742	0.000031	0.00115	1.668	-372E-7
62	0	105	0	0.05688	0.000540	0.00205	32.205	-242E-7
63	0	107	0	0.05658	0.000301	0.00236	1.793	-0.0003
64	0	108	0	0.05610	0.000477	0.00178	4.389	-0.0002
65	0	110	0	0.05598	0.000123	0.000626	1.256	-0.0002
66	0	112	0	0.05597	0.000013	0.000690	2.443	-11E-6
67	0	115	0	0.05517	0.000799	0.00409	131.7	-122E-7
68	0	117	0	0.05479	0.000379	0.000484	1.120	-0.0007
69	0	118	0	0.05466	0.000128	0.00549	10.000	-275E-7
70	0	119	0	0.05445	0.000213	0.00151	2.161	-0.0001
71	0	121	0	0.05441	0.000042	0.000696	1.143	-0.0001
72	0	123	0	0.05372	0.000688	0.00791	93.507	-112E-7
73	0	125	0	0.05344	0.000282	0.000566	1.288	-0.0004
74	0	126	0	0.05303	0.000404	0.00897	9.689	-0.0001
75	0	127	0	0.05243	0.000602	0.00367	2.308	-0.0004
76	0	129	0	0.05239	0.000038	0.000588	1.084	-0.0001
77	0	131	0	0.05225	0.000141	0.00659	39.678	-711E-8
78	0	132	0	0.05205	0.000196	0.000990	1.511	-0.0002
79	0	134	0	0.05164	0.000415	0.00933	10.898	-0.0001
80	0	135	0	0.05104	0.000602	0.000626	2.058	-0.0005
81	0	137	0	0.05098	0.000057	0.000809	1.207	-0.0001
82	0	139	0	0.05088	0.000105	0.00478	22.067	-955E-8
83	0	141	0	0.05060	0.000280	0.00387	2.962	-0.0002
84	0	143	0	0.04877	0.00183	0.00849	16.371	-0.0002
85	0	145	0	0.04859	0.000182	0.000871	1.000	-0.0003
86	0	147	0	0.04857	0.000020	0.00138	2.740	-142E-7
87	0	149	0	0.04836	0.000211	0.00177	18.600	-228E-7
88	0	151	0	0.04788	0.000478	0.00199	3.899	-0.0003
89	0	152	0	0.04718	0.000695	0.00214	3.152	-0.0004
90	0	154	0	0.04700	0.000187	0.000968	1.356	-0.0003
91	0	156	0	0.04699	8.492E-6	0.000540	1.554	-11E-6
92	0	158	0	0.04690	0.000093	0.00477	37.095	-504E-8
93	0	159	0	0.04676	0.000138	0.000871	1.325	-0.0002
94	0	160	0	0.04655	0.000212	0.00489	4.160	-0.0001
95	0	162	0	0.04584	0.000702	0.0101	4.453	-0.0003
96	0	164	0	0.04564	0.000205	0.000397	1.388	-0.0003
97	0	166	0	0.04563	8.358E-6	0.00138	4.463	-374E-8
98	0	169	0	0.04487	0.000759	0.00545	120.1	-125E-7
99	0	170	0	0.04428	0.000588	0.00236	1.775	-0.0011
100	0	172	0	0.04406	0.000219	0.00152	1.413	-0.0003
101	0	174	0	0.04146	0.00260	0.00156	40.057	-0.0001
102	0	176	0	0.04120	0.000264	0.000451	1.223	-0.0005
103	0	178	0	0.04118	0.000019	0.000447	1.555	-244E-7
104	0	179	0	0.04116	0.000022	0.000471	4.846	-1E-5
105	0	180	0	0.04115	7.352E-6	0.000827	10.000	-516E-8
106	0	182	0	0.04110	0.000050	0.000442	2.496	-397E-7
107	0	184	0	0.04060	0.000503	0.000337	17.977	-56E-6
108	0	186	0	0.04059	3.087E-6	0.000336	1.875	-331E-8
109	0	189	0	0.04053	0.000063	0.00707	53.631	-288E-8
110	0	190	0	0.04043	0.000101	0.000692	1.032	-0.0002
111	0	192	0	0.04037	0.000065	0.00481	2.573	-504E-7

112	0	194	0	0.03978	0.000589	0.00136	15.885	-0.0001
113	0	196	0	0.03977	9.458E-6	0.000233	1.236	-15E-6
114	0	198	0	0.03977	2.135E-6	0.000208	2.540	-168E-8
115	0	200	0	0.03976	0.000010	0.00184	14.836	-138E-8
116	0	202	0	0.03969	0.000067	0.00244	7.981	-167E-7
117	0	204	0	0.03932	0.000364	0.00278	9.270	-0.0001
118	0	206	0	0.03930	0.000024	0.000241	1.080	-431E-7
119	0	208	0	0.03930	1.155E-6	0.000348	3.301	-699E-9
120	0	211	0	0.03925	0.000045	0.00231	60.150	-15E-7
121	0	212	0	0.03920	0.000055	0.000872	1.652	-0.0001
122	0	213	0	0.03912	0.000080	0.00202	6.629	-207E-7
123	0	215	0	0.03872	0.000397	0.00527	7.591	-0.0001
124	0	217	0	0.03848	0.000242	0.000372	1.713	-0.0003
125	0	219	0	0.03848	9.245E-7	0.000173	1.249	-148E-8
126	0	221	0	0.03847	4.1E-6	0.000819	29.763	-275E-9
127	0	222	0	0.03847	7.103E-6	0.000170	1.335	-768E-8
128	0	223	0	0.03846	0.000011	0.000957	2.218	-801E-8
129	0	225	0	0.03839	0.000067	0.00353	7.403	-18E-6
130	0	227	0	0.03820	0.000186	0.000112	4.218	-0.0001
131	0	229	0	0.03820	1.855E-7	0.000087	1.292	-287E-9
132	0	232	0	0.03820	5.998E-6	0.000294	135.1	-89E-9
133	0	233	0	0.03819	5.358E-6	0.000228	1.477	-102E-7
134	0	235	0	0.03819	1.487E-6	0.000107	1.738	-171E-8
135	0	238	0	0.03816	0.000030	0.000201	59.983	-124E-8
136	0	240	0	0.03816	8.023E-7	0.000110	1.409	-114E-8
137	0	241	0	0.03816	5.68E-7	0.000226	5.289	-379E-9
138	0	243	0	0.03816	1.847E-7	0.000044	1.111	-332E-9
139	0	245	0	0.03816	1.663E-6	0.000771	99.827	-33E-9
140	0	246	0	0.03815	1.98E-6	0.000111	1.417	-293E-8
141	0	248	0	0.03815	6.908E-6	0.00140	34.225	-404E-9
142	0	249	0	0.03814	0.000011	0.000057	1.353	-128E-7
143	0	250	0	0.03812	0.000016	0.00187	3.386	-811E-8
144	0	252	0	0.03804	0.000080	0.00331	6.504	-246E-7
145	0	254	0	0.03801	0.000030	0.000073	1.453	-415E-7
146	0	255	0	0.03801	3.05E-7	0.000193	10.000	-75E-9
147	0	258	0	0.03800	6.288E-6	0.000235	26.399	-578E-9
148	0	260	0	0.03799	0.000015	0.000379	2.256	-139E-7
149	0	262	0	0.03794	0.000049	0.000593	11.529	-858E-8
150	0	264	0	0.03794	2.908E-6	0.000025	1.061	-547E-8
151	0	266	0	0.03794	2.06E-8	0.000026	2.650	-16E-9
152	0	269	0	0.03793	2.505E-6	0.000404	236.0	-21E-9
153	0	270	0	0.03793	2.36E-6	0.000083	1.350	-464E-8
154	0	272	0	0.03793	4.186E-7	0.000027	1.627	-515E-9
155	0	275	0	0.03790	0.000033	0.000290	204.2	-321E-9
156	0	277	0	0.03790	1.092E-6	0.000034	1.043	-209E-8
157	0	279	0	0.03790	5.96E-8	0.000047	5.330	-22E-9
158	0	282	0	0.03790	1.431E-6	0.000091	30.881	-96E-9
159	0	284	0	0.03790	2.441E-7	0.000113	2.504	-195E-9
160	0	286	0	0.03789	3.525E-6	0.000538	22.313	-273E-9
161	0	287	0	0.03789	4.357E-6	0.00148	4.511	-195E-8
162	0	288	0	0.03788	7.036E-6	0.000063	2.561	-425E-8
163	0	290	0	0.03788	2.27E-6	0.000435	1.460	-31E-7
164	0	292	0	0.03788	4.058E-7	9.035E-6	1.559	-52E-8

### Optimization Results

Iterations	164	Function Calls	293
Gradient Calls	232	Active Constraints	0
Objective Function	0.0378779129	Max Abs Gradient Element	9.0354545E-6
Slope of Search Direction	-5.202293E-7		

ABSGCONV convergence criterion satisfied.

---

BMI and Health: Use the Double Measurement Design  
Full Model

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#### The CALIS Procedure Covariance Structure Analysis: Maximum Likelihood Estimation

Fit Function	0.0379
Goodness of Fit Index (GFI)	0.9926
GFI Adjusted for Degrees of Freedom (AGFI)	0.9591
Root Mean Square Residual (RMR)	19.4718
Parsimonious GFI (Mulaik, 1989)	0.2206
Chi-Square	18.9011
Chi-Square DF	10
Pr > Chi-Square	0.0415
Independence Model Chi-Square	4015.9
Independence Model Chi-Square DF	45
RMSEA Estimate	0.0422
RMSEA 90% Lower Confidence Limit	0.0081
RMSEA 90% Upper Confidence Limit	0.0711
ECVI Estimate	0.2223
ECVI 90% Lower Confidence Limit	0.2051
ECVI 90% Upper Confidence Limit	0.2554
Probability of Close Fit	0.6316
Bentler's Comparative Fit Index	0.9978
Normal Theory Reweighted LS Chi-Square	18.6927
Akaike's Information Criterion	-1.0989
Bozdogan's (1987) CAIC	-53.2450
Schwarz's Bayesian Criterion	-43.2450
McDonald's (1989) Centrality	0.9911
Bentler & Bonett's (1980) Non-normed Index	0.9899
Bentler & Bonett's (1980) NFI	0.9953
James, Mulaik, & Brett (1982) Parsimonious NFI	0.2212
Z-Test of Wilson & Hilferty (1931)	1.7350
Bollen (1986) Normed Index Rho1	0.9788
Bollen (1988) Non-normed Index Delta2	0.9978
Hoelter's (1983) Critical N	485

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BMI and Health: Use the Double Measurement Design  
Full Model

8

The CALIS Procedure  
Covariance Structure Analysis: Maximum Likelihood Estimation

Manifest Variable Equations with Estimates

```
age1      =  1.0000 Fage      +  1.0000 delta11
bmi1     =  1.0000 Fbmi      +  1.0000 delta12
fat1     =  1.0000 Ffat      +  1.0000 delta13
cholest1 =  1.0000 Fcholest +  1.0000 eps11
diastol1 =  1.0000 Fdiastol +  1.0000 eps12
age2      =  1.0000 Fage      +  1.0000 delta21
bmi2     =  1.0000 Fbmi      +  1.0000 delta22
fat2     =  1.0000 Ffat      +  1.0000 delta23
cholest2 =  1.0000 Fcholest +  1.0000 eps21
diastol2 =  1.0000 Fdiastol +  1.0000 eps22
```

---

BMI and Health: Use the Double Measurement Design  
Full Model

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The CALIS Procedure  
Covariance Structure Analysis: Maximum Likelihood Estimation

Latent Variable Equations with Estimates

```
Fcholest =  0.1480*Fage      + -1.2703*Fbmi      +  2.2271*Ffat
Std Err   0.2128 gamma11      1.6550 gamma12      0.8974 gamma13
t Value   0.6957             -0.7675            2.4818

                           +  1.0000 e1

Fdiastol =  0.0104*Fage      + -0.1054*Fbmi      +  1.2692*Ffat
Std Err   0.0458 gamma21      0.3941 gamma22      0.2044 gamma23
t Value   0.2268             -0.2675            6.2090

                           +  1.0000 e2
```

### Variances of Exogenous Variables

Variable	Parameter	Estimate	Standard Error	t Value
Fage	phill	148.12838	9.79411	15.12
Fbmi	phi22	12.54181	0.94050	13.34
Ffat	phi33	46.99750	3.28849	14.29
e1	psi11	2391	161.53168	14.81
e2	psi22	75.69775	8.78257	8.62
eps11	TE1_11	195.80618	54.03321	3.62
eps12	TE1_22	207.71308	15.24803	13.62
eps21	TE2_11	336.03140	56.74542	5.92
eps22	TE2_22	25.20654	7.67288	3.29
delta11	TD1_11	22.30517	3.22022	6.93
delta12	TD1_22	8.61051	0.71704	12.01
delta13	TD1_33	13.95514	1.71930	8.12
delta21	TD2_11	6.30433	2.90105	2.17
delta22	TD2_22	1.28485	0.48547	2.65
delta23	TD2_33	11.46363	1.67508	6.84

### Covariances Among Exogenous Variables

Var1	Var2	Parameter	Estimate	Standard Error	t Value
Fage	Fbmi	phi12	8.53524	2.14246	3.98
Fage	Ffat	phi13	28.67293	4.20356	6.82
Fbmi	Ffat	phi23	21.07021	1.58695	13.28
e1	e2	psi12	26.99445	23.13516	1.17
eps11	eps12	TE1_12	2.37369	17.44389	0.14
eps21	eps22	TE2_12	10.55839	12.14484	0.87
eps11	delta11	TDE1_11	1.46571	9.28626	0.16
eps12	delta11	TDE1_12	5.50639	4.26027	1.29
eps11	delta12	TDE1_21	-1.68780	4.05537	-0.42
eps12	delta12	TDE1_22	8.22814	2.38542	3.45
delta11	delta12	TD1_12	2.41139	1.00109	2.41
eps11	delta13	TDE1_31	-1.67949	6.62998	-0.25
eps12	delta13	TDE1_32	0.90570	3.57876	0.25
delta11	delta13	TD1_13	-1.23726	1.62183	-0.76
delta12	delta13	TD1_23	8.07727	0.96844	8.34
eps21	delta21	TDE2_11	0.83261	9.02367	0.09
eps22	delta21	TDE2_12	2.24903	2.78751	0.81
eps21	delta22	TDE2_21	0.09756	3.34404	0.03
eps22	delta22	TDE2_22	2.97256	1.44467	2.06
delta21	delta22	TD2_12	0.26655	0.76726	0.35
eps21	delta23	TDE2_31	-4.03672	6.65942	-0.61
eps22	delta23	TDE2_32	2.33466	2.56252	0.91
delta21	delta23	TD2_13	1.97235	1.51921	1.30
delta22	delta23	TD2_23	0.06895	0.74323	0.09

BMI and Health: Use the Double Measurement Design  
Full Model

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The CALIS Procedure  
Covariance Structure Analysis: Maximum Likelihood Estimation

Manifest Variable Equations with Standardized Estimates

```
age1      =  0.9323 Fage      +  0.3618 delta11
bmil     =  0.7700 Fbmi      +  0.6380 delta12
fat1     =  0.8781 Ffat      +  0.4785 delta13
cholest1 =  0.9636 Fcholest +  0.2673 eps11
diastoll1 =  0.6433 Fdiastol +  0.7656 eps12
age2     =  0.9794 Fage      +  0.2020 delta21
bmi2     =  0.9524 Fbmi      +  0.3048 delta22
fat2     =  0.8966 Ffat      +  0.4428 delta23
cholest2 =  0.9399 Fcholest +  0.3415 eps21
diastol2 =  0.9238 Fdiastol +  0.3830 eps22
```

---

BMI and Health: Use the Double Measurement Design  
Full Model

11

The CALIS Procedure  
Covariance Structure Analysis: Maximum Likelihood Estimation

Latent Variable Equations with Standardized Estimates

```
Fcholest =  0.0357*Fage      + -0.0892*Fbmi      +  0.3027*Ffat
                gamma11           gamma12           gamma13
                               +  0.9695 e1

Fdiastol =  0.0104*Fage      + -0.0308*Fbmi      +  0.7185*Ffat
                gamma21           gamma22           gamma23
                               +  0.7184 e2
```

#### Squared Multiple Correlations

	Variable	Error Variance	Total Variance	R-Square
1	age1	22.30517	170.43356	0.8691
2	bmil	8.61051	21.15232	0.5929
3	fat1	13.95514	60.95264	0.7710
4	cholest1	195.80618	2740	0.9285
5	diastoll1	207.71308	354.37056	0.4139
6	age2	6.30433	154.43272	0.9592
7	bmi2	1.28485	13.82666	0.9071

8	fat2	11.46363	58.46113	0.8039
9	cholest2	336.03140	2881	0.8833
10	diastol2	25.20654	171.86402	0.8533
11	Fcholest	2391	2545	0.0602
12	Fdiastol	75.69775	146.65747	0.4838

#### Correlations Among Exogenous Variables

Var1	Var2	Parameter	Estimate
Fage	Fbmi	phi12	0.19802
Fage	Ffat	phi13	0.34365
Fbmi	Ffat	phi23	0.86786
e1	e2	psi12	0.06345
eps11	eps12	TE1_12	0.01177
eps21	eps22	TE2_12	0.11472
eps11	delta11	TDE1_11	0.02218
eps12	delta11	TDE1_12	0.08090
eps11	delta12	TDE1_21	-0.04110
eps12	delta12	TDE1_22	0.19456
delta11	delta12	TD1_12	0.17400
eps11	delta13	TDE1_31	-0.03213
eps12	delta13	TDE1_32	0.01682
delta11	delta13	TD1_13	-0.07013
delta12	delta13	TD1_23	0.73686
eps21	delta21	TDE2_11	0.01809
eps22	delta21	TDE2_12	0.17841
eps21	delta22	TDE2_21	0.00470
eps22	delta22	TDE2_22	0.52233
delta21	delta22	TD2_12	0.09366
eps21	delta23	TDE2_31	-0.06504
eps22	delta23	TDE2_32	0.13734
delta21	delta23	TD2_13	0.23201
delta22	delta23	TD2_23	0.01796

Skipping a lot of output, just give the optimization results and some of the parameter estimates.

### Optimization Results

Iterations	158	Function Calls	284
Gradient Calls	223	Active Constraints	2
Objective Function	0.0391401498	Max Abs Gradient Element	9.9301853E-6
Slope of Search Direction	-4.894672E-8		

ABSGCONV convergence criterion satisfied.

**WARNING:** There are 2 active constraints at the solution. The standard errors and Chi-Square test statistic assume the solution is located in the interior of the parameter space and hence do not apply if it is likely that some different set of inequality constraints could be active.

**NOTE:** The degrees of freedom are increased by the number of active constraints (see Dijkstra, 1992). The number of parameters in calculating fit indices is decreased by the number of active constraints. To turn off the adjustment, use the NOADJDF option.

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BMI and Health: Use the Double Measurement Design Reduced Model for testing BMI on both DVs	19
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#### The CALIS Procedure Covariance Structure Analysis: Maximum Likelihood Estimation

Fit Function	0.0391
Goodness of Fit Index (GFI)	0.9924
GFI Adjusted for Degrees of Freedom (AGFI)	0.9650
Root Mean Square Residual (RMR)	19.7718
Parsimonious GFI (Mulaik, 1989)	0.2646
Chi-Square	19.5309
Chi-Square DF	12
Pr > Chi-Square	0.0765

Skipping some more ...

#### The CALIS Procedure Covariance Structure Analysis: Maximum Likelihood Estimation

##### Latent Variable Equations with Estimates

Fcholest =	0.1987*Fage + 0*Fbmi + 1.6003*Ffat
Std Err	0.2018 gamma11 0 gamma12 0.3681 gamma13
t Value	0.9845 . 4.3477
	+ 1.0000 e1

Fdiastol =	0.0149*Fage + 0*Fbmi + 1.2178*Ffat
Std Err	0.0425 gamma21 0 gamma22 0.0798 gamma23
t Value	0.3500 . 15.2689
	+ 1.0000 e2

## Variances of Exogenous Variables

Skipping another couple of pages ...

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BMI and Health: Use the Double Measurement Design  
Calculate Likelihood ratio test of H0: gamma12=gamma22=0

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G

0.6311185  
PVAL

0.7293809