

STA 2101/442 Formulas

$$Z_1 = \frac{\sqrt{n}(\bar{Y}_n - \pi_0)}{\sqrt{\pi_0(1-\pi_0)}} \quad Z_2 = \frac{\sqrt{n}(\bar{Y}_n - \pi_0)}{\sqrt{\bar{Y}_n(1-\bar{Y}_n)}} \quad \bar{Y}_n \pm z_{\alpha/2} \sqrt{\frac{\bar{Y}_n(1-\bar{Y}_n)}{n}}$$

> qnorm(0.975)
[1] 1.959964
> qnorm(0.995)
[1] 2.575829

If $E(\mathbf{X}) = \boldsymbol{\mu}$, then $V(\mathbf{X})$ is defined by $V(\mathbf{X}) = E\{(\mathbf{X} - \boldsymbol{\mu})(\mathbf{X} - \boldsymbol{\mu})'\}$.

If $\mathbf{X} \sim N(\boldsymbol{\mu}, \boldsymbol{\Sigma})$, then $\mathbf{AX} \sim N(\mathbf{A}\boldsymbol{\mu}, \mathbf{A}\boldsymbol{\Sigma}\mathbf{A}')$.

If $\lim_{n \rightarrow \infty} E(T_n) = \theta$ and $\lim_{n \rightarrow \infty} Var(T_n) = 0$, then $T_n \xrightarrow{P} \theta$

$$\mathbf{Y}_n = \sqrt{n}(\bar{\mathbf{X}}_n - \boldsymbol{\mu}) \xrightarrow{d} \mathbf{Y} \sim N(\mathbf{0}, \boldsymbol{\Sigma}) \quad \sqrt{n}(g(\mathbf{T}_n) - g(\boldsymbol{\theta})) \xrightarrow{d} \dot{g}(\boldsymbol{\theta})\mathbf{T}, \quad \dot{g}(\mathbf{x}) = \left[\frac{\partial g_i}{\partial x_j} \right]_{k \times d}$$

$$P(n_1, \dots, n_c) = \binom{n}{n_1 \dots n_c} \pi_1^{n_1} \cdots \pi_c^{n_c} \quad L(\boldsymbol{\pi}) = \prod_{i=1}^n \pi_1^{y_{i,1}} \pi_2^{y_{i,2}} \cdots \pi_c^{y_{i,c}} = \pi_1^{n_1} \pi_2^{n_2} \cdots \pi_c^{n_c}$$

$$G^2 = -2 \log \left(\frac{\max_{\theta \in \Theta_0} L(\theta)}{\max_{\theta \in \Theta} L(\theta)} \right) \quad W_n = (\mathbf{L}\widehat{\boldsymbol{\theta}}_n - \mathbf{h})' \left(\mathbf{L}\widehat{\mathbf{V}}_n \mathbf{L}' \right)^{-1} (\mathbf{L}\widehat{\boldsymbol{\theta}}_n - \mathbf{h})$$

If $X \sim N(\mu, \sigma^2)$, then $\frac{X^2}{\sigma^2} \sim \chi^2(1, \lambda)$, with $\lambda = \frac{\mu^2}{\sigma^2}$

$$\widehat{\boldsymbol{\beta}} = (\mathbf{X}'\mathbf{X})^{-1}\mathbf{X}'\mathbf{Y} \sim N_p(\boldsymbol{\beta}, \sigma^2(\mathbf{X}'\mathbf{X})^{-1}) \quad SSE/\sigma^2 \sim \chi^2(n-p)$$

$$F = \frac{(\mathbf{L}\widehat{\boldsymbol{\beta}} - \mathbf{h})'(\mathbf{L}(\mathbf{X}'\mathbf{X})^{-1}\mathbf{L}')^{-1}(\mathbf{L}\widehat{\boldsymbol{\beta}} - \mathbf{h})}{r MSE_F} = \frac{(SSR_F - SSR_R)/r}{MSE_F} = \left(\frac{n-p}{r} \right) \left(\frac{a}{1-a} \right), \text{ where } a = \frac{R_F^2 - R_R^2}{1 - R_R^2} = \frac{rF}{n-p+rF}$$

$$\phi = \frac{(\mathbf{L}\boldsymbol{\beta} - \mathbf{h})'(\mathbf{L}(\mathbf{X}'\mathbf{X})^{-1}\mathbf{L}')^{-1}(\mathbf{L}\boldsymbol{\beta} - \mathbf{h})}{\sigma^2}$$

$$f(y|\theta, \phi) = \exp \left\{ \frac{y\theta - b(\theta)}{\phi} + c(y, \phi) \right\} \quad \theta = g(\mu) = \eta = \mathbf{x}'\boldsymbol{\beta}$$

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> df = 1:8
> CriticalValue = qchisq(0.95,df)
> round(rbind(df,CriticalValue),3)
      [,1]   [,2]   [,3]   [,4]   [,5]   [,6]   [,7]   [,8]
df       1.000  2.000  3.000  4.000  5.00  6.000  7.000  8.000
CriticalValue 3.841  5.991  7.815  9.488 11.07 12.592 14.067 15.507
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