

# BMI Health Study

## Naive Regression

```
***** bmil.sas *****
options linesize=79 noovp formdlim=' ';
title 'BMI and Health: Read data and analyze ignoring measurement error';

data health;
  infile 'bmihealth2.data';
  input age1 bmi1 fat1 cholest1 diastol1
        age2 bmi2 fat2 cholest2 diastol2;
  /* fat1 and fat2 are percent body fat */
  age = (age1+age2)/2; bmi = (bmi1+bmi2)/2; fat = (fat1+fat2)/2;
  cholest = (cholest1+cholest2)/2 ; diastol = (diastol1+diastol2)/2;

proc means;
  var age1 -- diastol;

proc reg;
  title2 'Regression on average measurements';
  model cholest diastol = age bmi fat;
  BMI: mtest bmi=0; /* Multivariate test */
```

BMI and Health: Read data and analyze ignoring measurement error 1

### The MEANS Procedure

| Variable | N   | Mean        | Std Dev    | Minimum     | Maximum     |
|----------|-----|-------------|------------|-------------|-------------|
| age1     | 500 | 44.1300000  | 12.9561114 | 3.0000000   | 80.0000000  |
| bmi1     | 500 | 25.4786000  | 4.6790543  | 12.8000000  | 39.4000000  |
| fat1     | 500 | 19.4780000  | 7.7567319  | 0           | 44.6000000  |
| cholest1 | 500 | 263.8172000 | 55.7074960 | 113.4000000 | 440.3000000 |
| diastol1 | 500 | 88.5940000  | 18.0461767 | 16.0000000  | 146.0000000 |
| age2     | 500 | 45.5820000  | 12.4130352 | 6.0000000   | 78.0000000  |
| bmi2     | 500 | 25.6574000  | 3.7869522  | 14.3000000  | 37.1000000  |
| fat2     | 500 | 19.4778000  | 7.4274451  | 0           | 45.8000000  |
| cholest2 | 500 | 265.3700000 | 56.7716240 | 106.0000000 | 445.6000000 |
| diastol2 | 500 | 89.3420000  | 13.2834459 | 52.0000000  | 131.0000000 |
| age      | 500 | 44.8560000  | 12.4336824 | 4.5000000   | 79.0000000  |
| bmi      | 500 | 25.5680000  | 3.9567218  | 13.9000000  | 37.2000000  |
| fat      | 500 | 19.4779000  | 7.1693749  | 0           | 44.8500000  |
| cholest  | 500 | 264.5936000 | 55.0124311 | 118.6500000 | 442.9500000 |
| diastol  | 500 | 88.9680000  | 13.7890628 | 39.5000000  | 132.5000000 |

The REG Procedure  
 Model: MODEL1  
 Dependent Variable: cholest

|                             |     |
|-----------------------------|-----|
| Number of Observations Read | 500 |
| Number of Observations Used | 500 |

#### Analysis of Variance

| Source          | DF  | Sum of Squares | Mean Square | F Value | Pr > F |
|-----------------|-----|----------------|-------------|---------|--------|
| Model           | 3   | 146506         | 48835       | 17.76   | <.0001 |
| Error           | 496 | 1363651        | 2749.29688  |         |        |
| Corrected Total | 499 | 1510157        |             |         |        |

|                |           |          |        |
|----------------|-----------|----------|--------|
| Root MSE       | 52.43374  | R-Square | 0.0970 |
| Dependent Mean | 264.59360 | Adj R-Sq | 0.0916 |
| Coeff Var      | 19.81671  |          |        |

#### Parameter Estimates

| Variable  | DF | Parameter Estimate | Standard Error | t Value | Pr >  t |
|-----------|----|--------------------|----------------|---------|---------|
| Intercept | 1  | 220.06103          | 21.01086       | 10.47   | <.0001  |
| age       | 1  | -0.27139           | 0.20017        | -1.36   | 0.1758  |
| bmi       | 1  | 0.51641            | 1.01541        | 0.51    | 0.6113  |
| fat       | 1  | 2.23342            | 0.57920        | 3.86    | 0.0001  |

BMI and Health: Read data and analyze ignoring measurement error  
Regression on average measurements

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The REG Procedure  
Model: MODEL1  
Dependent Variable: diastol

Number of Observations Read 500  
Number of Observations Used 500

Analysis of Variance

| Source          | DF  | Sum of Squares | Mean Square | F Value | Pr > F |
|-----------------|-----|----------------|-------------|---------|--------|
| Model           | 3   | 31627          | 10542       | 82.67   | <.0001 |
| Error           | 496 | 63252          | 127.52449   |         |        |
| Corrected Total | 499 | 94879          |             |         |        |
| Root MSE        |     | 11.29267       | R-Square    | 0.3333  |        |
| Dependent Mean  |     | 88.96800       | Adj R-Sq    | 0.3293  |        |
| Coeff Var       |     | 12.69296       |             |         |        |

Parameter Estimates

| Variable  | DF | Parameter Estimate | Standard Error | t Value | Pr >  t |
|-----------|----|--------------------|----------------|---------|---------|
| Intercept | 1  | 49.69194           | 4.52512        | 10.98   | <.0001  |
| age       | 1  | 0.12648            | 0.04311        | 2.93    | 0.0035  |
| bmi       | 1  | 0.82627            | 0.21869        | 3.78    | 0.0002  |
| fat       | 1  | 0.64056            | 0.12474        | 5.14    | <.0001  |

BMI and Health: Read data and analyze ignoring measurement error  
Regression on average measurements

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The REG Procedure  
Model: MODEL1  
Multivariate Test: BMI

Multivariate Statistics and Exact F Statistics

S=1 M=0 N=246.5

| Statistic              | Value      | F Value | Num DF | Den DF | Pr > F |
|------------------------|------------|---------|--------|--------|--------|
| Wilks' Lambda          | 0.97130971 | 7.31    | 2      | 495    | 0.0007 |
| Pillai's Trace         | 0.02869029 | 7.31    | 2      | 495    | 0.0007 |
| Hotelling-Lawley Trace | 0.02953773 | 7.31    | 2      | 495    | 0.0007 |
| Roy's Greatest Root    | 0.02953773 | 7.31    | 2      | 495    | 0.0007 |

## Measurement Error Regression

```
//***** bmi2.sas *****
options linesize=79 pagesize = 500 noovp formdlim='_' ;
title 'BMI and Health: Use the Double Measurement Design';

data health;
    infile 'bmihealth2.data'; /* bmihealth2.data is a big improvement */
    input age1 bmil fat1 cholest1 diastol1
          age2 bmid fat2 cholest2 diastol2;
    /* fat1 and fat2 are percent body fat */
    age = (age1+age2)/2; bmi = (bmil+bmid)/2; fat = (fat1+fat2)/2;
    cholest = (cholest1+cholest2)/2 ; diastol = (diastol1+diastol2)/2;

/* Exclude some output you really don't want to see. */
ods exclude Calis.ML.SqMultCorr (persist);

proc calis pshort nostand pcorr;
    /* Analyze covariance matrix is now default. pshort and
       nostand suppresses some output. pcorr prints
       correlation (or covariance) matrices of observed
       variables -- both sample and predicted. */

title2 'Full Model';
var /* Name the observed variables */
    age1 bmil fat1 cholest1 diastol1
    age2 bmid fat2 cholest2 diastol2;

/* Now give simultaneous equations, separated by commas. Latent
   variables begin with F for factor. Error terms begin with
   E for error or D for disturbance. SAS is not case sensitive.
   You must name all the parameters. Optional starting values in
   parentheses may be given after the parameters. */
lineqs
    Fcholest = beta11 Fage + beta12 Fbmi + beta13 Ffat + epsilon1,
    Fdiastol = beta21 Fage + beta22 Fbmi + beta23 Ffat + epsilon2,
    age1      = Fage + e11, bmil = Fbmi + e12,
    fat1      = Ffat + e13,
    cholest1  = Fcholest + e14, diastol1 = Fdiastol + e15,
    age2      = Fage + e21, bmid = Fbmi + e22,
    fat2      = Ffat + e23,
    cholest2  = Fcholest + e24, diastol2 = Fdiastol + e25;
variance /* Variances of exogenous vars */
    Fage = phill, Fbmi = phi22, Ffat = phi33,
    epsilon1 = psill, epsilon2 = psi22,
    e11 = omega111, e12 = omega122, e13 = omega133,
    e14 = omega144, e15 = omega155,
    e21 = omega211, e22 = omega222, e23 = omega233,
    e24 = omega244, e25 = omega255;
cov /* Covariances */
    Fage Fbmi = phi12, Fage Ffat = phi13, Fbmi Ffat = phi23,
    epsilon1 epsilon2 = psi12,
    e11 e12 = omega112, e11 e13 = omega113, e11 e14 = omega114,
    e11 e15 = omega115,
    e12 e13 = omega123, e12 e14 = omega124, e12 e15 = omega125,
    e13 e14 = omega134, e13 e15 = omega135,
    e14 e15 = omega145,
    e21 e22 = omega212, e21 e23 = omega213, e21 e24 = omega214,
    e21 e25 = omega215,
    e22 e23 = omega223, e22 e24 = omega224, e22 e25 = omega225,
    e23 e24 = omega234, e23 e25 = omega235,
    e24 e25 = omega245;
```

```

bounds /* Variances are positive */
    0.0 < phill phi22 phi33 psill psi22
        omega111 omega122 omega133 omega144 omega155
        omega211 omega222 omega233 omega244 omega255;

/* Now fit a reduced model to test H0: beta12 = beta22 = 0,
meaning BMI is unrelated to either cholesterol or blood pressure
if we allow for age and percent body fat. Copy the code; only
the last line is different. */

proc calis pshort nostand;
  title2 'Reduced Model with beta12=beta22=0';
  var /* Name the observed variables */
      age1 bmi1 fat1 cholest1 diastol1
      age2 bmi2 fat2 cholest2 diastol2;
  /* Now give simultaneous equations, separated by commas. Latent
variables begin with F for factor. Error terms begin with
E for error or D for disturbance. SAS is not case sensitive.
You must name all the parameters. Optional starting values in
parentheses may be given after the parameters. */
  lineqs
    Fcholest = beta11 Fage + beta12 Fbmi + beta13 Ffat + epsilon1,
    Fdiastol = beta21 Fage + beta22 Fbmi + beta23 Ffat + epsilon2,
    age1      = Fage + e11, bmi1 = Fbmi + e12,
    fat1      = Ffat + e13,
    cholest1  = Fcholest + e14, diastol1 = Fdiastol + e15,
    age2      = Fage + e21, bmi2      = Fbmi + e22,
    fat2      = Ffat + e23,
    cholest2  = Fcholest + e24, diastol2 = Fdiastol + e25;
  variance /* Variances of exogenous vars */
    Fage = phill, Fbmi = phi22, Ffat = phi33,
    epsilon1 = psill, epsilon2 = psi22,
    e11 = omega111, e12 = omega122, e13 = omega133,
    e14 = omega144, e15 = omega155,
    e21 = omega211, e22 = omega222, e23 = omega233,
    e24 = omega244, e25 = omega255;
  cov /* Covariances */
    Fage Fbmi = phill, Fage Ffat = phi13, Fbmi Ffat = phi23,
    epsilon1 epsilon2 = psi12,
    e11 e12 = omega112, e11 e13 = omega113, e11 e14 = omega114,
    e11 e15 = omega115,
    e12 e13 = omega123, e12 e14 = omega124, e12 e15 = omega125,
    e13 e14 = omega134, e13 e15 = omega135,
    e14 e15 = omega145,
    e21 e22 = omega212, e21 e23 = omega213, e21 e24 = omega214,
    e21 e25 = omega215,
    e22 e23 = omega223, e22 e24 = omega224, e22 e25 = omega225,
    e23 e24 = omega234, e23 e25 = omega235,
    e24 e25 = omega245;
  bounds /* Variances are positive */
    0.0 < phill phi22 phi33 psill psi22
        omega111 omega122 omega133 omega144 omega155
        omega211 omega222 omega233 omega244 omega255;
  lincon beta12=0, beta22=0;

proc iml;
  title2 'Calculate Likelihood ratio test of H0: beta12=beta22=0';
  G = 500 * (0.0122914464 - 0.0093074908);
  /* Difference between final objective function values */
  pval = 1 - probchi(G,2);
  print G pval;
  print "Or, difference between 'Chi-Square' values";
  diff = 6.1334-4.6444;
  print "6.1334-4.6444 = " diff;

```

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BMI and Health: Use the Double Measurement Design  
Full Model

1

The CALIS Procedure  
Covariance Structure Analysis: Model and Initial Values

Modeling Information

|                |             |
|----------------|-------------|
| Data Set       | WORK.HEALTH |
| N Records Read | 500         |
| N Records Used | 500         |
| N Obs          | 500         |
| Model Type     | LINEQS      |
| Analysis       | Covariances |

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BMI and Health: Use the Double Measurement Design  
Full Model

2

The CALIS Procedure  
Covariance Structure Analysis: Descriptive Statistics

Covariance Matrix (DF = 499)

|          | age1      | bmi1     | fat1      | cholest1  | diastol1  |
|----------|-----------|----------|-----------|-----------|-----------|
| age1     | 167.86082 | 8.93946  | 26.05437  | 19.08533  | 48.31741  |
| bmi1     | 8.93946   | 21.89355 | 29.77223  | 56.71544  | 35.65743  |
| fat1     | 26.05437  | 29.77223 | 60.16689  | 124.49070 | 54.39786  |
| cholest1 | 19.08533  | 56.71544 | 124.49070 | 3103.3251 | 123.97594 |
| diastol1 | 48.31741  | 35.65743 | 54.39786  | 123.97594 | 325.66449 |
| age2     | 148.22078 | 5.03573  | 23.54229  | 21.03486  | 37.65761  |
| bmi2     | 3.62158   | 13.19402 | 20.61349  | 61.58983  | 25.59028  |
| fat2     | 25.29808  | 21.42201 | 45.13296  | 130.30870 | 57.56051  |
| cholest2 | 8.13778   | 54.87651 | 110.89557 | 2889.5639 | 120.65613 |
| diastol2 | 34.64884  | 24.38168 | 55.62858  | 104.79631 | 129.21929 |

Covariance Matrix (DF = 499)

|          | age2      | bmi2     | fat2      | cholest2  | diastol2  |
|----------|-----------|----------|-----------|-----------|-----------|
| age1     | 148.22078 | 3.62158  | 25.29808  | 8.13778   | 34.64884  |
| bmi1     | 5.03573   | 13.19402 | 21.42201  | 54.87651  | 24.38168  |
| fat1     | 23.54229  | 20.61349 | 45.13296  | 110.89557 | 55.62858  |
| cholest1 | 21.03486  | 61.58983 | 130.30870 | 2889.5639 | 104.79631 |
| diastol1 | 37.65761  | 25.59028 | 57.56051  | 120.65613 | 129.21929 |
| age2     | 154.08344 | 3.10881  | 22.26445  | 11.60828  | 36.93282  |
| bmi2     | 3.10881   | 14.34101 | 19.30298  | 57.02692  | 27.09416  |
| fat2     | 22.26445  | 19.30298 | 55.16694  | 114.17915 | 51.68196  |
| cholest2 | 11.60828  | 57.02692 | 114.17915 | 3223.0173 | 91.06699  |
| diastol2 | 36.93282  | 27.09416 | 51.68196  | 91.06699  | 176.44994 |

Determinant 4.5765674E18 Ln 42.967481

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BMI and Health: Use the Double Measurement Design  
Full Model

3

The CALIS Procedure  
Covariance Structure Analysis: Optimization

Levenberg-Marquardt Optimization

Scaling Update of More (1978)

|                          |    |
|--------------------------|----|
| Parameter Estimates      | 45 |
| Functions (Observations) | 55 |
| Lower Bounds             | 15 |
| Upper Bounds             | 0  |

Optimization Start

|                          |              |                    |              |
|--------------------------|--------------|--------------------|--------------|
| Active Constraints       | 0            | Objective Function | 0.2768223813 |
| Max Abs Gradient Element | 0.1013655982 | Radius             | 1            |

| Iter | Rest<br>arts | Func<br>Calls | Act<br>Con | Objective<br>Function | Obj<br>Change | Max Abs<br>Gradient<br>Element | Lambda | Actual<br>Over<br>Pred<br>Change |
|------|--------------|---------------|------------|-----------------------|---------------|--------------------------------|--------|----------------------------------|
|      |              |               |            |                       |               |                                |        |                                  |
| 1    | 0            | 6             | 0          | 0.10492               | 0.1719        | 0.0424                         | 0      | 0.674                            |
| 2    | 0            | 8             | 0          | 0.01737               | 0.0875        | 0.00443                        | 0      | 1.073                            |
| 3    | 0            | 10            | 0          | 0.00932               | 0.00805       | 0.000201                       | 0      | 1.093                            |
| 4    | 0            | 12            | 0          | 0.00931               | 0.000013      | 0.000164                       | 0      | 1.019                            |
| 5    | 0            | 14            | 0          | 0.00931               | 5.719E-8      | 1.441E-6                       | 0      | 1.025                            |

Optimization Results

|                           |                     |                          |              |
|---------------------------|---------------------|--------------------------|--------------|
| Iterations                | 5                   | Function Calls           | 17           |
| Jacobian Calls            | 7                   | Active Constraints       | 0            |
| <b>Objective Function</b> | <b>0.0093074908</b> | Max Abs Gradient Element | 1.4407197E-6 |
| Lambda                    | 0                   | Actual Over Pred Change  | 1.0254675652 |
| Radius                    | 0.0018060845        |                          |              |

Convergence criterion (ABSGCONV=0.00001) satisfied.

BMI and Health: Use the Double Measurement Design  
Full Model

4

The CALIS Procedure  
Covariance Structure Analysis: Maximum Likelihood Estimation

Fit Summary

|                |                                  |               |
|----------------|----------------------------------|---------------|
| Modeling Info  | N Observations                   | 500           |
|                | N Variables                      | 10            |
|                | N Moments                        | 55            |
|                | N Parameters                     | 45            |
|                | N Active Constraints             | 0             |
|                | Baseline Model Function Value    | 8.1272        |
|                | Baseline Model Chi-Square        | 4055.4515     |
|                | Baseline Model Chi-Square DF     | 45            |
|                | Pr > Baseline Model Chi-Square   | <.0001        |
| Absolute Index | Fit Function                     | 0.0093        |
|                | <b>Chi-Square</b>                | <b>4.6444</b> |
|                | <b>Chi-Square DF</b>             | <b>10</b>     |
|                | <b>Pr &gt; Chi-Square</b>        | <b>0.9136</b> |
|                | Z-Test of Wilson & Hilferty      | -1.3642       |
|                | Hoelter Critical N               | 1967          |
|                | Root Mean Square Residual (RMSR) | 5.7999        |
|                | Standardized RMSR (SRMSR)        | 0.0114        |
|                | Goodness of Fit Index (GFI)      | 0.9982        |

|                   |                                  |          |
|-------------------|----------------------------------|----------|
| Parsimony Index   | Adjusted GFI (AGFI)              | 0.9899   |
|                   | Parsimonious GFI                 | 0.2218   |
|                   | RMSEA Estimate                   | 0.0000   |
|                   | RMSEA Lower 90% Confidence Limit | 0.0000   |
|                   | RMSEA Upper 90% Confidence Limit | 0.0184   |
|                   | Probability of Close Fit         | 0.9987   |
|                   | ECVI Estimate                    | 0.1937   |
|                   | ECVI Lower 90% Confidence Limit  | 0.2049   |
|                   | ECVI Upper 90% Confidence Limit  | 0.2079   |
|                   | Akaike Information Criterion     | 94.6444  |
|                   | Bozdogan CAIC                    | 329.3018 |
|                   | Schwarz Bayesian Criterion       | 284.3018 |
| Incremental Index | McDonald Centrality              | 1.0054   |
|                   | Bentler Comparative Fit Index    | 1.0000   |
|                   | Bentler-Bonett NFI               | 0.9989   |
|                   | Bentler-Bonett Non-normed Index  | 1.0060   |
|                   | Bollen Normed Index Rho1         | 0.9948   |
|                   | Bollen Non-normed Index Delta2   | 1.0013   |
|                   | James et al. Parsimonious NFI    | 0.2220   |

#### Predicted Covariances

|          | age1             | bmi1            | fat1             | cholest1         | diastol1         |
|----------|------------------|-----------------|------------------|------------------|------------------|
| age1     | 166.24694        | 8.17463         | 25.76119         | 21.96533         | 46.18388         |
| bmi1     | 8.17463          | 22.04955        | 30.00458         | 61.34375         | 34.86877         |
| fat1     | 25.76119         | 30.00458        | 60.73126         | 132.38341        | 53.44883         |
| cholest1 | 21.96533         | 61.34375        | 132.38341        | 3103.6215        | 108.72072        |
| diastol1 | 46.18388         | 34.86877        | 53.44883         | 108.72072        | 324.01763        |
| age2     | <b>147.62538</b> | <b>4.16880</b>  | <b>23.36704</b>  | <b>19.25674</b>  | <b>35.60086</b>  |
| bmi2     | <b>4.16880</b>   | <b>13.36758</b> | <b>21.01792</b>  | <b>62.22916</b>  | <b>24.78849</b>  |
| fat2     | <b>23.36704</b>  | <b>21.01792</b> | <b>44.57431</b>  | <b>124.44423</b> | <b>56.38255</b>  |
| cholest2 | <b>19.25674</b>  | <b>62.22916</b> | <b>124.44423</b> | <b>2903.1136</b> | <b>108.81759</b> |
| diastol2 | <b>35.60086</b>  | <b>24.78849</b> | <b>56.38255</b>  | <b>108.81759</b> | <b>128.58644</b> |

#### Predicted Covariances

|          | age2             | bmi2            | fat2             | cholest2         | diastol2         |
|----------|------------------|-----------------|------------------|------------------|------------------|
| age1     | <b>147.62538</b> | <b>4.16880</b>  | <b>23.36704</b>  | <b>19.25674</b>  | <b>35.60086</b>  |
| bmi1     | <b>4.16880</b>   | <b>13.36758</b> | <b>21.01792</b>  | <b>62.22916</b>  | <b>24.78849</b>  |
| fat1     | <b>23.36704</b>  | <b>21.01792</b> | <b>44.57431</b>  | <b>124.44423</b> | <b>56.38255</b>  |
| cholest1 | <b>19.25674</b>  | <b>62.22916</b> | <b>124.44423</b> | <b>2903.1136</b> | <b>108.81759</b> |
| diastol1 | <b>35.60086</b>  | <b>24.78849</b> | <b>56.38255</b>  | <b>108.81759</b> | <b>128.58644</b> |
| age2     | 154.50002        | 3.50674         | 20.65811         | 17.28984         | 37.87862         |
| bmi2     | 3.50674          | 14.45915        | 19.16469         | 59.57095         | 27.44593         |
| fat2     | 20.65811         | 19.16469        | 53.92456         | 113.04535        | 51.53445         |
| cholest2 | 17.28984         | 59.57095        | 113.04535        | 3248.2548        | 99.82594         |
| diastol2 | 37.87862         | 27.44593        | 51.53445         | 99.82594         | 177.03207        |

Determinant 4.6193627E18      Ln 42.976788

The CALIS Procedure  
Covariance Structure Analysis: Maximum Likelihood Estimation

Linear Equations

Fcholest = -0.3197\*Fage + 0.3935\*Fbmi + 2.7739\*Ffat  
Std Err 0.2280 beta11 1.7096 beta12 0.9814 beta13  
t Value -1.4024 0.2302 2.8264  
+ 1.0000 epsilon1

Linear Equations

Fdiastol = 0.0204\*Fage + -0.4795\*Fbmi + 1.4803\*Ffat  
Std Err 0.0501 beta21 0.4192 beta22 0.2348 beta23  
t Value 0.4066 -1.1440 6.3059  
+ 1.0000 epsilon2

Linear Equations

age1 = 1.0000 Fage + 1.0000 e11

Linear Equations

bmi1 = 1.0000 Fbmi + 1.0000 e12

Linear Equations

fat1 = 1.0000 Ffat + 1.0000 e13

Linear Equations

cholest1 = 1.0000 Fcholest + 1.0000 e14

Linear Equations

diastol1 = 1.0000 Fdiastol + 1.0000 e15

Linear Equations

age2 = 1.0000 Fage + 1.0000 e21

Linear Equations

bmi2 = 1.0000 Fbmi + 1.0000 e22

Linear Equations

fat2 = 1.0000 Ffat + 1.0000 e23

Linear Equations

cholest2 = 1.0000 Fcholest + 1.0000 e24

Linear Equations

diasitol2 = 1.0000 Fdiasitol + 1.0000 e25

Estimates for Variances of Exogenous Variables

| Variable Type | Variable | Parameter | Estimate  | Standard Error | t Value  |
|---------------|----------|-----------|-----------|----------------|----------|
| Latent        | Fage     | phi11     | 147.62538 | 9.72823        | 15.17495 |
|               | Fbmi     | phi22     | 13.36758  | 0.98913        | 13.51443 |
|               | Ffat     | phi33     | 44.57431  | 3.11040        | 14.33072 |
| Disturbance   | epsilon1 | psi11     | 2540      | 171.77281      | 14.78457 |
|               | epsilon2 | psi22     | 56.28249  | 9.24845        | 6.08561  |
| Error         | e11      | omegal11  | 18.62155  | 2.92259        | 6.37158  |
|               | e12      | omegal12  | 8.68196   | 0.71007        | 12.22696 |
|               | e13      | omegal13  | 16.15695  | 1.66444        | 9.70712  |
|               | e14      | omegal14  | 200.50786 | 57.59459       | 3.48137  |
|               | e15      | omegal15  | 195.43119 | 14.36626       | 13.60348 |
|               | e21      | omegab11  | 6.87464   | 2.70919        | 2.53753  |
|               | e22      | omegab22  | 1.09156   | 0.49224        | 2.21755  |
|               | e23      | omegab33  | 9.35025   | 1.54338        | 6.05828  |
|               | e24      | omegab44  | 345.14117 | 60.47109       | 5.70754  |
|               | e25      | omegab55  | 48.44563  | 8.27042        | 5.85770  |

Covariances Among Exogenous Variables

| Var1     | Var2     | Parameter | Estimate  | Standard Error | t Value  |
|----------|----------|-----------|-----------|----------------|----------|
| Fage     | Fbmi     | phi12     | 4.16880   | 2.14702        | 1.94166  |
| Fage     | Ffat     | phi13     | 23.36704  | 3.99758        | 5.84529  |
| Fbmi     | Ffat     | phi23     | 21.01792  | 1.58854        | 13.23095 |
| epsilon1 | epsilon2 | psi12     | -45.95363 | 25.04350       | -1.83495 |
| e11      | e12      | omegal12  | 4.00583   | 0.94772        | 4.22683  |
| e11      | e13      | omegal13  | 2.39415   | 1.50990        | 1.58564  |
| e11      | e14      | omegal14  | 2.70859   | 9.11878        | 0.29703  |
| e11      | e15      | omegal15  | 10.58302  | 3.83545        | 2.75927  |
| e12      | e13      | omegal23  | 8.98666   | 0.95884        | 9.37242  |
| e12      | e14      | omegal24  | -0.88540  | 4.19082        | -0.21127 |
| e12      | e15      | omegal25  | 10.08028  | 2.28090        | 4.41944  |
| e13      | e14      | omegal34  | 7.93918   | 6.76172        | 1.17414  |
| e13      | e15      | omegal35  | -2.93372  | 3.41941        | -0.85796 |

|     |     |          |           |          |          |
|-----|-----|----------|-----------|----------|----------|
| e14 | e15 | omega145 | -0.09687  | 16.95779 | -0.00571 |
| e21 | e22 | omega212 | -0.66206  | 0.73717  | -0.89811 |
| e21 | e23 | omega213 | -2.70893  | 1.37336  | -1.97248 |
| e21 | e24 | omega214 | -1.96690  | 8.98900  | -0.21881 |
| e21 | e25 | omega215 | 2.27776   | 2.71807  | 0.83801  |
| e22 | e23 | omega223 | -1.85323  | 0.70700  | -2.62127 |
| e22 | e24 | omega224 | -2.65821  | 3.48688  | -0.76234 |
| e22 | e25 | omega225 | 2.65744   | 1.49113  | 1.78216  |
| e23 | e24 | omega234 | -11.39888 | 6.56616  | -1.73600 |
| e23 | e25 | omega235 | -4.84810  | 2.54402  | -1.90568 |
| e24 | e25 | omega245 | -8.99165  | 12.64259 | -0.71122 |

---

BMI and Health: Use the Double Measurement Design  
Reduced Model with beta12=beta22=0

6

The CALIS Procedure  
Covariance Structure Analysis: Model and Initial Values

Modeling Information

|                |             |
|----------------|-------------|
| Data Set       | WORK.HEALTH |
| N Records Read | 500         |
| N Records Used | 500         |
| N Obs          | 500         |
| Model Type     | LINEQS      |
| Analysis       | Covariances |

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BMI and Health: Use the Double Measurement Design  
Reduced Model with beta12=beta22=0

7

The CALIS Procedure  
Covariance Structure Analysis: Optimization

Levenberg-Marquardt Optimization

Scaling Update of More (1978)

|                          |    |
|--------------------------|----|
| Parameter Estimates      | 45 |
| Functions (Observations) | 55 |
| Lower Bounds             | 15 |
| Upper Bounds             | 0  |
| Linear Constraints       | 2  |

Optimization Start

|                          |              |                    |              |
|--------------------------|--------------|--------------------|--------------|
| Active Constraints       | 2            | Objective Function | 0.4178440369 |
| Max Abs Gradient Element | 0.3660107658 | Radius             | 1            |

| Iter | Rest arts | Func Calls | Act Con | Objective Function | Obj Fun Change | Max Abs Gradient Element | Actual Over Pred Change |       |
|------|-----------|------------|---------|--------------------|----------------|--------------------------|-------------------------|-------|
|      |           |            |         |                    |                |                          | Lambda                  |       |
| 1    | 0         | 4          | 2       | 0.02411            | 0.3937         | 0.0180                   | 0                       | 0.983 |
| 2    | 0         | 6          | 2       | 0.01233            | 0.0118         | 0.00354                  | 0                       | 1.088 |
| 3    | 0         | 8          | 2       | 0.01229            | 0.000037       | 0.000266                 | 0                       | 1.032 |
| 4    | 0         | 10         | 2       | 0.01229            | 2.904E-7       | 0.000035                 | 0                       | 1.043 |
| 5    | 0         | 12         | 2       | 0.01229            | 2.601E-9       | 2.183E-6                 | 0                       | 1.047 |

### Optimization Results

|                    |              |                          |              |
|--------------------|--------------|--------------------------|--------------|
| Iterations         | 5            | Function Calls           | 15           |
| Jacobian Calls     | 7            | Active Constraints       | 2            |
| Objective Function | 0.0122914464 | Max Abs Gradient Element | 2.183169E-6  |
| Lambda             | 0            | Actual Over Pred Change  | 1.0474386893 |
| Radius             | 0.0002628856 |                          |              |

Convergence criterion (ABSGCONV=0.00001) satisfied.

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BMI and Health: Use the Double Measurement Design  
Reduced Model with beta12=beta22=0

8

The CALIS Procedure  
Covariance Structure Analysis: Maximum Likelihood Estimation

#### Fit Summary

|                 |                                  |           |
|-----------------|----------------------------------|-----------|
| Modeling Info   | N Observations                   | 500       |
|                 | N Variables                      | 10        |
|                 | N Moments                        | 55        |
|                 | N Parameters                     | 43        |
|                 | N Active Constraints             | 0         |
|                 | Baseline Model Function Value    | 8.1272    |
|                 | Baseline Model Chi-Square        | 4055.4515 |
|                 | Baseline Model Chi-Square DF     | 45        |
|                 | Pr > Baseline Model Chi-Square   | <.0001    |
|                 | Fit Function                     | 0.0123    |
| Absolute Index  | Chi-Square                       | 6.1334    |
|                 | Chi-Square DF                    | 12        |
|                 | Pr > Chi-Square                  | 0.9092    |
|                 | Z-Test of Wilson & Hilferty      | -1.3370   |
|                 | Hoelter Critical N               | 1711      |
| Parsimony Index | Root Mean Square Residual (RMSR) | 6.0164    |
|                 | Standardized RMSR (SRMSR)        | 0.0117    |
|                 | Goodness of Fit Index (GFI)      | 0.9975    |
|                 | Adjusted GFI (AGFI)              | 0.9887    |
|                 | Parsimonious GFI                 | 0.2660    |
|                 | RMSEA Estimate                   | 0.0000    |

**Skipping the rest ...**

---

BMI and Health: Use the Double Measurement Design  
Calculate Likelihood ratio test of H0: beta12=beta22=0

10

G pval

1.4919778 0.4742651

Or, difference between 'Chi-Square' values

diff

6.1334-4.6444 = 1.489

```

***** bmi3.sas *****
options linesize=79 pagesize = 500 noovp formdlim='_' ;
title 'BMI and Health: Like bmi2.sas, but try to make it shorter';
title2 'Also Try Wald Test: Compare G2 = 1.49, df=2, p = 0.47';

data health;
  infile 'bmihealth2.data';
  input age1 bmi1 fat1 cholest1 diastol1
        age2 bmi2 fat2 cholest2 diastol2;
  /* fat1 and fat2 are percent body fat */
  age = (age1+age2)/2; bmi = (bmi1+bmi2)/2; fat = (fat1+fat2)/2;
  cholest = (cholest1+cholest2)/2 ; diastol = (diastol1+diastol2)/2;

/* Exclude some output you really don't want to see. */
ods exclude Calis.ML.SqMultCorr (persist);

proc calis pshort nostand pcorr;
  title2 'Full Model';
  var   /* Name the observed variables */
        age1 bmi1 fat1 cholest1 diastol1
        age2 bmi2 fat2 cholest2 diastol2;
  lineqs
    Fcholest = beta11 Fage + beta12 Fbmi + beta13 Ffat + epsilon1,
    Fdiastol = beta21 Fage + beta22 Fbmi + beta23 Ffat + epsilon2,
    age1      = Fage + e11, bmi1 = Fbmi + e12,
    fat1      = Ffat + e13,
    cholest1 = Fcholest + e14, diastol1 = Fdiastol + e15,
    age2      = Fage + e21, bmi2      = Fbmi + e22,
    fat2      = Ffat + e23,
    cholest2 = Fcholest + e24, diastol2 = Fdiastol + e25;
  variance /* Variances of exogenous vars will be
            called v-something. __ means fill in the numbers. */
            Fage Fbmi Ffat epsilon1 epsilon2 e11-e15 e21-e25 = 15 * v__ ;
  cov   /* Covariances: If not mentioned, it's zero. */
            Fage Ffat Fbmi = 3 * phi__, epsilon1 epsilon2 = psi12 ,
            e11-e15 = 10 * omega1__, e21-e25 = 10 * omega2__;
  /* If you don't count the variances and covariances you get a warning.
     It's better to count them. */
  bounds 0.0 < v01-v15; /* Variances are positive */
  /* Wald test of H0: beta12=beta22=0 */
  simtests BMI = [f1 f2];
  f1 = beta12;
  f2 = beta22;

```

## Output is the same except for things like

### Estimates for Variances of Exogenous Variables

| Variable Type | Variable | Parameter | Estimate  | Standard Error | t Value  |
|---------------|----------|-----------|-----------|----------------|----------|
| Latent        | Fage     | v01       | 147.62538 | 9.72823        | 15.17495 |
|               | Fbmi     | v02       | 13.36758  | 0.98913        | 13.51443 |
|               | Ffat     | v03       | 44.57431  | 3.11040        | 14.33072 |
| Disturbance   | epsilon1 | v04       | 2540      | 171.77281      | 14.78457 |
|               | epsilon2 | v05       | 56.28249  | 9.24845        | 6.08561  |
| Error         | e11      | v06       | 18.62155  | 2.92259        | 6.37158  |
|               | e12      | v07       | 8.68196   | 0.71007        | 12.22696 |
|               | e13      | v08       | 16.15695  | 1.66444        | 9.70712  |
|               | e14      | v09       | 200.50786 | 57.59459       | 3.48137  |
|               | e15      | v10       | 195.43119 | 14.36626       | 13.60348 |
|               | e21      | v11       | 6.87464   | 2.70919        | 2.53753  |
|               | e22      | v12       | 1.09156   | 0.49224        | 2.21755  |
|               | e23      | v13       | 9.35025   | 1.54338        | 6.05828  |

|     |     |           |          |         |
|-----|-----|-----------|----------|---------|
| e24 | v14 | 345.14117 | 60.47109 | 5.70754 |
| e25 | v15 | 48.44563  | 8.27042  | 5.85770 |

#### Covariances Among Exogenous Variables

| Var1     | Var2     | Parameter | Estimate  | Standard Error | t Value  |
|----------|----------|-----------|-----------|----------------|----------|
| Fage     | Ffat     | phi1      | 23.36704  | 3.99758        | 5.84529  |
| Fage     | Fbmi     | phi2      | 4.16880   | 2.14702        | 1.94166  |
| Ffat     | Fbmi     | phi3      | 21.01792  | 1.58854        | 13.23095 |
| epsilon1 | epsilon2 | psi12     | -45.95363 | 25.04350       | -1.83495 |
| e11      | e12      | omega101  | 4.00583   | 0.94772        | 4.22683  |
| e11      | e13      | omega102  | 2.39415   | 1.50990        | 1.58564  |
| e12      | e13      | omega103  | 8.98666   | 0.95884        | 9.37242  |
| e11      | e14      | omega104  | 2.70859   | 9.11878        | 0.29703  |

**Skipping ...**

#### Simultaneous Tests

| Simultaneous Test | Parametric Function | Function Value | DF | Chi-Square | p Value |
|-------------------|---------------------|----------------|----|------------|---------|
| BMI               | f1                  | 0.39355        | 2  | 1.35941    | 0.5068  |
|                   | f2                  | -0.47951       | 1  | 0.05299    | 0.8179  |
|                   |                     |                | 1  | 1.30863    | 0.2526  |

**Repeating output from above ...**

#### Full Model

The CALIS Procedure  
Covariance Structure Analysis: Maximum Likelihood Estimation

#### Linear Equations

|            |                   |               |               |
|------------|-------------------|---------------|---------------|
| Fcholest = | -0.3197*Fage      | + 0.3935*Fbmi | + 2.7739*Ffat |
| Std Err    | 0.2280            | beta11 1.7096 | beta12 0.9814 |
| t Value    | -1.4024           | 0.2302        | beta13 2.8264 |
|            | + 1.0000 epsilon1 |               |               |

#### Linear Equations

|            |                   |                |               |
|------------|-------------------|----------------|---------------|
| Fdiastol = | 0.0204*Fage       | + -0.4795*Fbmi | + 1.4803*Ffat |
| Std Err    | 0.0501            | beta21 0.4192  | beta22 0.2348 |
| t Value    | 0.4066            | -1.1440        | beta23 6.3059 |
|            | + 1.0000 epsilon2 |                |               |

> **1.1440^2**  
[1] 1.308736