Sample Questions: Expected Value, Variance and Covariance

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1. Let X have a continuous uniform distribution on (L, R). Calculate E(X).

2. Recall that a fair game is one with expected value zero. You wager one dollar, and toss a coin with $P(\text{Head}) = \theta$. If it's heads, you win. In dollars, what should the payoff be so that the game is fair?

3. Let $X \sim \text{Poisson}(\lambda)$. Calculate E(X).

- 4. Let the continuous random variable X have density $f_X(x) = \begin{cases} \frac{\alpha}{x^{\alpha+1}} & \text{for } x \ge 1\\ 0 & \text{otherwise} \end{cases}$ Where $\alpha > 0$.
 - (a) Verify that $f_{X}(x)$ integrates to one.

(b) Calculate E(X). For what values of α does E(X) exist?

5. Let $X \sim N(\mu, \sigma^2)$. Calculate E(X).

6. Let X have a Gamma distribution with parameters α and λ . Calculate $E(X^k)$. 7. Prove $Var(bX) = b^2 Var(X)$.

8. Show $Var(X) = E(X^2) - [E(X)]^2$.

9. Let X have density e^{-x} for $x \ge 0$ and zero otherwise. Calculate Var(X).

10. Let $X \sim N(\mu, \sigma^2)$. Calculate Var(X).

11. Show Cov(X, Y) = E(XY) - E(X)E(Y).

12. Let X and Y be independent (continuous) random variables. Show E(XY) = E(X)E(Y).

13. If X and Y are independent, Cov(X, Y) =

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http://www.utstat.toronto.edu/~brunner/oldclass/256f19