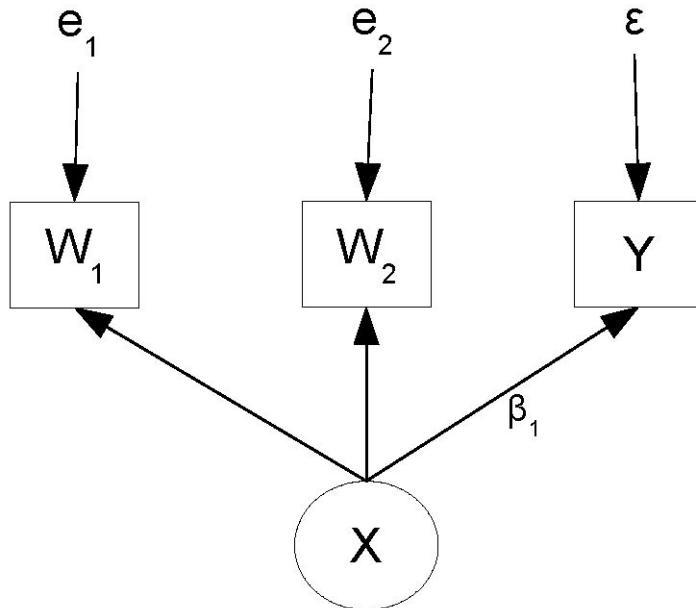


Little Double Measurement Regression Example*



```

> rm(list=ls()); options(scipen=999)
> # install.packages("lavaan", dependencies = TRUE) # Only need to do this once
> library(lavaan)
This is lavaan 0.6-11
lavaan is FREE software! Please report any bugs.
>
> babydouble =
read.table("http://www.utstat.toronto.edu/~brunner/openSEM/data/Babydouble.data.txt")
> head(babydouble)
   W1     W2     Y
1 9.94 12.24 15.23
2 12.42 11.32 14.55
3 10.43 10.40 12.40
4 9.07  9.85 17.09
5 11.04 11.98 16.83
6 10.40 10.85 15.04

> dim(babydouble)
[1] 150    3

> summary(babydouble)
      W1          W2          Y        
Min. : 6.190  Min. : 6.76  Min. : 3.98 
1st Qu.: 8.932 1st Qu.: 9.11  1st Qu.:10.97 
Median : 9.720 Median :10.05  Median :13.22 
Mean   : 9.809 Mean  :10.06  Mean  :13.10 
3rd Qu.:10.655 3rd Qu.:10.99 3rd Qu.:15.46 
Max.   :12.830 Max.  :13.57  Max.  :21.62 

> cor(babydouble)
      W1          W2          Y        
W1  1.0000000  0.5748331  0.1714324 
W2  0.5748331  1.0000000  0.1791539 
Y   0.1714324  0.1791539  1.0000000
  
```

* Copyright information is on the last page.

```

>
> dmodel1 = 'Y ~ beta1*X          # Latent variable model (even though Y is observed)
+   X =~ 1*W1 + 1*W2      # Measurement model
+   # Variances (covariances would go here too)
+   X~~phi*X            # Var(X) = phi
+   Y~~psi*Y            # Var(epsilon) = psi
+   W1~~omegal*W1        # Var(e1) = omegal
+   W2~~omega2*W2        # Var(e2) = omega2
+
> dfit1 = lavaan(dmodel1, data=babydouble)
> summary(dfit1)

```

lavaan 0.6-11 ended normally after 23 iterations

Estimator	ML
Optimization method	NLMINB
Number of model parameters	5

Number of observations	150
------------------------	-----

Model Test User Model:

Test statistic	0.007
Degrees of freedom	1
P-value (Chi-square)	0.933

Parameter Estimates:

Standard errors	Standard
Information	Expected
Information saturated (h1) model	Structured

Latent Variables:

	Estimate	Std.Err	z-value	P(> z)
X =~				
W1	1.000			
W2	1.000			

Regressions:

	Estimate	Std.Err	z-value	P(> z)
Y ~				
X (bet1)	0.707	0.290	2.442	0.015

Variances:

	Estimate	Std.Err	z-value	P(> z)
X (phi)	1.104	0.181	6.104	0.000
.Y (psi)	9.775	1.153	8.481	0.000
.W1 (omg1)	0.834	0.158	5.265	0.000
.W2 (omg2)	0.800	0.156	5.123	0.000

```

>
> parameterEstimates(dfit1)
   lhs op rhs  label    est     se      z pvalue ci.lower ci.upper
1   Y ~   X  betal  0.707  0.290  2.442  0.015   0.140   1.275
2   X == W1          1.000  0.000    NA     NA   1.000   1.000
3   X == W2          1.000  0.000    NA     NA   1.000   1.000
4   X ~~ X  phi   1.104  0.181  6.104  0.000   0.750   1.459
5   Y ~~ Y  psi   9.775  1.153  8.481  0.000   7.516  12.034
6  W1 ~~ W1 omega1  0.834  0.158  5.265  0.000   0.524   1.145
7  W2 ~~ W2 omega2  0.800  0.156  5.123  0.000   0.494   1.105

> parTable(dfit1)
  id lhs op rhs user block group free ustart exo  label plabel start    est     se
1  1  Y ~   X   1     1     1     1     NA   0  betal   .p1. 0.000  0.707  0.290
2  2  X == W1   1     1     1     0     1   0  .p2. 1.000  1.000  0.000
3  3  X == W2   1     1     1     0     1   0  .p3. 1.000  1.000  0.000
4  4  X ~~ X   1     1     1     2     NA   0  phi    .p4. 0.050  1.104  0.181
5  5  Y ~~ Y   1     1     1     3     NA   0  psi    .p5. 5.164  9.775  1.153
6  6  W1 ~~ W1   1     1     1     4     NA   0 omega1 .p6. 0.968  0.834  0.158
7  7  W2 ~~ W2   1     1     1     5     NA   0 omega2 .p7. 0.953  0.800  0.156

> coef(dfit1) # A vector of MLEs
beta1   phi   psi omega1 omega2
0.707  1.104  9.775  0.834  0.800

> fitted(dfit1) # Sigma(thetahat) and mu(thetahat)
$cov
   W1     W2      Y
W1  1.939
W2  1.104  1.904
Y   0.781  0.781 10.327

>
> vcov(dfit1)
   beta1   phi   psi   omega1 omega2
beta1  0.084
phi   -0.007  0.033
psi   -0.035  0.002  1.328
omega1 0.003 -0.004 -0.002  0.025
omega2 0.003 -0.005 -0.002 -0.007  0.024

> logLik(dfit1)
'log Lik.' -878.512 (df=5)

```

```

> # Fit a restricted model (restricted by H0)
> dfit1r = lavaan(dmodel1, data=babydouble, constraints = 'omegal==omega2')
> anova(dfit1r,dfit1)

Chi-Squared Difference Test

      Df   AIC     BIC   Chisq Chisq diff Df diff Pr(>Chisq)
dfit1    1 1767 1782.1 0.0071
dfit1r   2 1765 1777.1 0.0262    0.019189       1      0.8898

> # Put multiple constraints on separate lines, like this.
> dfit1r2 = lavaan(dmodel1, data=babydouble, constraints = 'omegal==omega2
+                   phi==1')

> anova(dfit1r2,dfit1)
Chi-Squared Difference Test

      Df   AIC     BIC   Chisq Chisq diff Df diff Pr(>Chisq)
dfit1    1 1767.0 1782.1 0.0071
dfit1r2  3 1763.4 1772.4 0.3868    0.37978       2      0.8271

>
> # For Wald tests: Wtest = function(L,Tn,Vn,h=0) # H0: L theta = h
> source("http://www.utstat.utoronto.ca/~brunner/Rfunctions/Wtest.txt")
> LL = cbind(0,0,0,1,-1); LL
[ ,1] [ ,2] [ ,3] [ ,4] [ ,5]
[1, ] 0 0 0 1 -1

> Wtest(LL,coef(dfit1),vcov(dfit1))
      W      df      p-value
0.01918586 1.00000000 0.88983498

> # Non-linear functions of the parameters with :=
> dmodel1b = 'Y ~ betal*X          # Latent variable model
+             X =~ 1*W1 + 1*W2      # Measurement model
+             # Variances (covariances would go here too)
+             X~~phi*X            # Var(X) = phi
+             Y~~psi*Y            # Var(epsilon) = psi
+             W1~~omegal*W1        # Var(e1) = omegal
+             W2~~omega2*W2        # Var(e2) = omega2
+             diff := omegal-omega2
+             rel1 := phi/(omegal+phi)
+
> dfit1b = lavaan(dmodel1b, data=babydouble)
> parameterEstimates(dfit1b)
   lhs op           rhs label   est     se    z pvalue ci.lower ci.upper
1   Y ~             X betal 0.707 0.290 2.442  0.015  0.140   1.275
2   X =~            W1          1.000 0.000   NA    NA  1.000   1.000
3   X =~            W2          1.000 0.000   NA    NA  1.000   1.000
4   X ~~            X   phi  1.104 0.181 6.104  0.000  0.750   1.459
5   Y ~~            Y   psi  9.775 1.153 8.481  0.000  7.516  12.034
6   W1 ~~           W1  omegal 0.834 0.158 5.265  0.000  0.524   1.145
7   W2 ~~           W2  omega2 0.800 0.156 5.123  0.000  0.494   1.105
8 diff := omegal-omega2 diff 0.035 0.252 0.139  0.890 -0.458   0.528
9 rel1 := phi/(omegal+phi) rel1 0.570 0.066 8.657  0.000  0.441   0.699

> sqrt(0.01918586) # Compare Z statistic for H0: omegal=omega2
[1] 0.138513

```

```

> # And one attempt to fit a non-identified model
>
> dmodel0 = 'Y ~ beta1*X      # Latent variable model (even though Y is observed)
+   X =~ 1*W1      # Measurement model
+   # Variances (covariances would go here too)
+   X~~phi*X      # Var(X) = phi
+   Y~~psi*Y      # Var(epsilon) = psi
+   W1~~omegal*W1 # Var(el) = omegal
+
> dfit0 = lavaan(dmodel0, data=babydouble)

Warning message:
In lav_model_vcov(lavmodel = lavmodel, lavsamplestats = lavsamplestats, :
lavaan WARNING:
  Could not compute standard errors! The information matrix could
  not be inverted. This may be a symptom that the model is not
  identified.

> summary(dfit0)
lavaan 0.6-11 ended normally after 17 iterations

Estimator                               ML
Optimization method                    NLMINB
Number of model parameters             4
Number of observations                  150

Model Test User Model:

Test statistic                           NA
Degrees of freedom                      -1
P-value (Unknown)                       NA

Parameter Estimates:

Standard errors                         Standard
Information                            Expected
Information saturated (h1) model        Structured

Latent Variables:
          Estimate Std.Err z-value P(>|z|)
X =~ W1           1.000

Regressions:
          Estimate Std.Err z-value P(>|z|)
Y ~ X       (bet1)    0.734     NA

Variances:
          Estimate Std.Err z-value P(>|z|)
X      (phi)    1.044     NA
.Y     (psi)    9.765     NA
.W1   (omg1)   0.892     NA

```

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<http://www.utstat.toronto.edu/brunner/oldclass/2053f22>